

# Compiler Construction 2018/19

## — Exercise Sheet 10 —

Hand in until January 7th, 2019 before the exercise class.

### Exercise 1

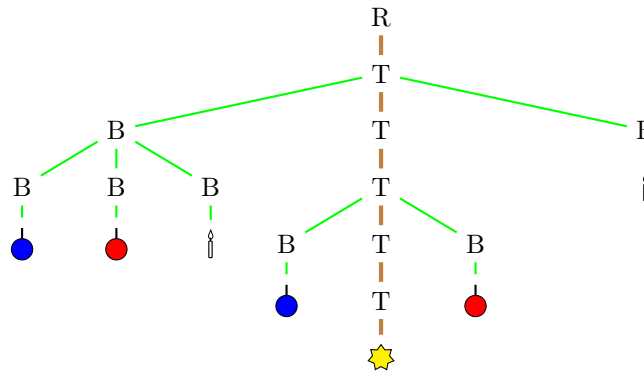
**(6 Points)**

In the following we consider a grammar  $G$  whose derivation tree visualizes a christmas tree.

Let  $G = (N, \Sigma, P, R)$  be the CFG with  $N = \{R, T, B\}$  and  $\Sigma = \{\star, \hat{\uparrow}, \bullet, \circ\}$ <sup>1</sup>. The productions  $P$  are as follows:

$$\begin{aligned}
 R &\rightarrow T \\
 T &\rightarrow BTB \mid T \mid \star \\
 B &\rightarrow BBB \mid BB \mid B \mid \hat{\uparrow} \mid \bullet \mid \circ
 \end{aligned}$$

An example christmas tree (upside down with the root at the top) would look as follows:



Give an attribute grammar  $\mathfrak{A} = (G, E, V)$  for  $G$  such that the obtained christmas trees (i.e., derivation trees) satisfy the following restrictions:

- (i) The distance from  $\star$  to the start symbol  $R$  is greater than the distance between every other leaf and  $R$ .
- (ii) The number of  $\hat{\uparrow}$  on the left and right hand side of the tree (split by the trunk  $T$ ) are equal.
- (iii) When traversing the tree in a pre-order manner the  $\bullet$  and  $\circ$  are encountered alternatingly and the first visited ornament is  $\bullet$ .

*Hint:* pre-order is a depth-first traversal where first the node, then the left subtree and last the right subtree are visited.

As before, you may use a synthesized Boolean attribute  $b$  such that: A word  $w$  is in the language of  $\mathfrak{A} = (G, E, V)$  iff  $w \in L(G)$  and, at the root of a derivation tree,  $b.0 = \text{true}$ .

The given example christmas tree satisfies all three restrictions as can be easily seen:

- (i) The distance from  $\star$  to the start symbol  $R$  is 6 whereas the largest other distance is 5.
- (ii) On the left hand side there is one  $\hat{\uparrow}$  and on the right hand side there is one  $\hat{\uparrow}$  as well.
- (iii) The traversal yields the following (correct) order of ornaments:  $\bullet, \circ, \bullet, \circ$ .

<sup>1</sup>For ease of notation you can also use  $\Sigma = \{\text{star}, \text{candle}, \text{red}, \text{blue}\}$ .

## Exercise 2

(4 Points)

Consider the following intermediate code:

```

      ⋮
2:  LIT(-1);
3:  LOAD(1, 3);    (dif, off)
4:  LT;
5:  JFALSE(7);
6:  CALL(6, 1, 3); (ca, dif, loc)
7:  RET;
  
```

Give the next four states of the abstract machine starting in:

$$(ca, d, p) := (3, 7 : -1, 6 : 5 : 42 : 6 : 6 : 6 : 7 : 6 : 30 : 1 : 2 : -3 : 4 : 9 : 3 : \dots)$$

Recall that the procedure stack has the form:

<i>sl</i>	<i>dl</i>	<i>ra</i>	$v_1$	$\dots$	$v_n$	$\dots$
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and the *base*-function is defined as:

$$\begin{aligned}
 base(p, 0) &:= 1 \\
 base(p, dif + 1) &:= base(p, dif) + p.base(p, dif)
 \end{aligned}$$

## Exercise 3

(4 Points)

In addition to `while`-loops we want to have `for`-loops with implicit declaration of the counter variable in our example programming language:

$$\text{for (var } X := A ; B ; C_1 ) C_2$$

- (a) Extend the translation function *ct* accordingly. You may assume that the variable *X* is already declared, i.e., it is *update*(*var X, st, l*) with *st* the symbol table and *l* the current level.
- (b) Generate intermediate code for

$$\text{for (var } x := 0 ; x < 10 ; x := x + 1 ) P()$$

without parameters for the CALL instruction generated for *P*().

*We wish you a merry Christmas and  
a Happy New Year!*