



# Semantics and Verification of Software

Winter Semester 2017/18

Lecture 19: Security Type Systems

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<http://moves.rwth-aachen.de/teaching/ws-1718/sv-sw/>

# Recap: Type Systems

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## Outline of Lecture 19

Recap: Type Systems

Language-Based Security

A Security Type System

# Recap: Type Systems

## Typed Execution of Statements

Definition (Typed execution of statements (cf. Definition 16.4))

$\rightarrow_1 \subseteq (Cmd \times \Sigma) \times (Cmd \times \Sigma)$  is given by:

$$\begin{array}{c} \frac{}{\langle \text{skip}, \sigma \rangle \rightarrow_1 \langle \downarrow, \sigma \rangle} \qquad \frac{\langle a, \sigma \rangle \rightarrow v}{\langle x := a, \sigma \rangle \rightarrow_1 \langle \downarrow, \sigma[x \mapsto v] \rangle} \\ \frac{\langle b, \sigma \rangle \rightarrow \text{true}}{\langle \text{if } b \text{ then } c_1 \text{ else } c_2 \text{ end}, \sigma \rangle \rightarrow_1 \langle c_1, \sigma \rangle} \qquad \frac{\langle c_1, \sigma \rangle \rightarrow_1 \langle c'_1, \sigma' \rangle}{\langle c_1; c_2, \sigma \rangle \rightarrow_1 \langle c'_1; c_2, \sigma' \rangle} \\ \dots \qquad \dots \end{array}$$

**Thus:** execution gets stuck iff expression evaluation gets stuck

### Example

For  $c = (x := x + 1)$ ,

- if  $\sigma(x) = 2 \in \mathbb{Z}$ , then  $\langle c, \sigma \rangle \rightarrow_1 \sigma[x \mapsto 3]$
- if  $\sigma(x) = 3.14 \in \mathbb{R}$ , then  $\langle c, \sigma \rangle \not\rightarrow_1$

# Recap: Type Systems

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## Data Types and Type Environments

- Data types

$$Typ = \{int, real\}$$

with  $\tau \in Typ$

- Observation: type of (arithmetic) expression depends on types of contained variables
- Therefore: introduce **type environments**

$$TEnv = \{\Gamma \mid \Gamma : Var \rightarrow Typ\}$$

- In the following: typing rule systems for

- arithmetic expression  $a \in AExp$  has type  $\tau \in Typ$ :
- Boolean expression  $b \in BExp$  is well-typed:
- statement  $c \in Cmd$  is well-typed:

$$\Gamma \vdash a : \tau$$

$$\Gamma \vdash b$$

$$\Gamma \vdash c$$

in type environment  $\Gamma \in TEnv$

# Recap: Type Systems

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## Typing Rules for Commands

### Definition (Well-typedness of commands)

For  $\Gamma \in TEnv$  and  $c \in Cmd$ ,  $\Gamma \vdash c$  is given by

$$\frac{}{\Gamma \vdash \text{skip}} \quad \frac{\Gamma \vdash a : \Gamma(x)}{\Gamma \vdash x := a} \quad \frac{\Gamma \vdash c_1 \quad \Gamma \vdash c_2}{\Gamma \vdash c_1 ; c_2}$$
$$\frac{\Gamma \vdash b \quad \Gamma \vdash c_1 \quad \Gamma \vdash c_2}{\Gamma \vdash \text{if } b \text{ then } c_1 \text{ else } c_2 \text{ end}} \quad \frac{\Gamma \vdash b \quad \Gamma \vdash c}{\Gamma \vdash \text{while } b \text{ do } c \text{ end}}$$

**Thus:** command not well-typed iff some expression not well-typed or assignment incompatible

# Recap: Type Systems

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## Type Soundness for Commands

### Theorem (Progress)

*If  $c \in \text{Cmd} \setminus \{\downarrow\}$ ,  $\sigma \in \Sigma$  and  $\Gamma \in \text{TEnv}$  such that  $\Gamma \vdash c$  and  $\Gamma \vdash \sigma$ , then there exist  $c' \in \text{Cmd}$  and  $\sigma' \in \Sigma$  such that  $\langle c, \sigma \rangle \rightarrow_1 \langle c', \sigma' \rangle$ .*

### Theorem (Preservation)

*If  $c, c' \in \text{Cmd}$ ,  $\sigma, \sigma' \in \Sigma$  and  $\Gamma \in \text{TEnv}$  such that  $\Gamma \vdash c$ ,  $\Gamma \vdash \sigma$  and  $\langle c, \sigma \rangle \rightarrow_1 \langle c', \sigma' \rangle$ , then  $\Gamma \vdash c'$  and  $\Gamma \vdash \sigma'$ .*

### Corollary (Type soundness)

*If  $c, c' \in \text{Cmd}$ ,  $\sigma, \sigma' \in \Sigma$  and  $\Gamma \in \text{TEnv}$  such that  $\Gamma \vdash c$ ,  $\Gamma \vdash \sigma$  and  $\langle c, \sigma \rangle \rightarrow_1^* \langle c', \sigma' \rangle$  with  $c' \neq \downarrow$ , then there exist  $c'' \in \text{Cmd}$  and  $\sigma'' \in \Sigma$  such that  $\langle c', \sigma' \rangle \rightarrow_1 \langle c'', \sigma'' \rangle$ .*

All proofs by rule induction (based on the corresponding results for expressions)

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## Language-Based Security

### Information flow control

Goal: Ensure that programs protect private data like passwords, bank details, or medical records. There should be no information flow from private data into public channels.



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Goal: Ensure that programs protect private data like passwords, bank details, or medical records. There should be no information flow from private data into public channels.

### Language-based security

Approach to information flow control where **data flow analysis** is used to determine whether a program is free of illicit information flows

- guarantees confidentiality by **program analysis**, not by cryptography
- analyses often expressed as **type systems**

## Security Levels

- Data objects (such as program variables) have **security/confidentiality levels**
- Security levels are **partially ordered**:

$l < l'$  means that  $l$  is less confidential than  $l'$

(thus, information is allowed to flow from  $l$  to  $l'$  but not vice versa)

- Simplest choice: **low** (low/public) and **high** (high/confidential/secret/private) with  $\text{low} < \text{high}$
- Extension to multi-level security by generalisation to **lattice**  $SL$
- Security levels of variables given by  $sl : \text{Var} \rightarrow SL$

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### Example 19.1 (Illicit flows)

Let  $sl(\text{low}) = \text{low}$  and  $sl(\text{high}) = \text{high}$ .

**Explicit:** `low := high`

**Implicit (“occlusion”):** `if high = 1 then low := 1 else low := 2 end`

## Security Levels on Expressions

The security level of an expression is the maximal security level of any of its variables.

### Definition 19.2 (Security levels on expressions)

$sl : Var \rightarrow SL$  is extended to  $sl : AExp \cup BExp \rightarrow SL$  as follows:

$$\begin{array}{ll} sl(z) = \min SL & sl(t) = \min SL \\ sl(a_1 + a_2) = sl(a_1) \sqcup sl(a_2) & sl(a_1 = a_2) = sl(a_1) \sqcup sl(a_2) \\ \dots & sl(\neg b) = sl(b) \\ & sl(b_1 \wedge b_2) = sl(b_1) \sqcup sl(b_2) \\ & \dots \end{array}$$

## Security Levels on States

Idea: identify when states can (not) be distinguished by a “low observer”

### Definition 19.3 (Security levels on states)

Two program states  $\sigma_1, \sigma_2 \in \Sigma$  **agree up to level**  $l \in SL$  if for all  $x \in Var$  such that  $sl(x) \leq l$ ,

$$\sigma_1(x) = \sigma_2(x).$$

Notation:  $\sigma_1 =_{\leq l} \sigma_2$  (analogously:  $\sigma_1 =_{< l} \sigma_2$ )

## Non-Interference Informally

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### Non-interference (informally)

Program  $c$  guarantees **non-interference** if for all states  $\sigma_1, \sigma_2$ : If  $\sigma_1$  and  $\sigma_2$  agree on low variables (but possibly differ on high variables), then the states resulting from executing  $\langle c, \sigma_1 \rangle$  and  $\langle c, \sigma_2 \rangle$  must also agree on low variables.

## Non-interference Formally

### Definition 19.4 (Non-interference)

Program  $c \in \mathit{Cmd}$  guarantees **non-interference** at security level  $l \in \mathit{SL}$  if for all  $\sigma_1, \sigma_2, \sigma'_1, \sigma'_2 \in \Sigma$ :

$$\sigma_1 =_{\leq l} \sigma_2, \langle c, \sigma_1 \rangle \rightarrow \sigma'_1, \langle c, \sigma_2 \rangle \rightarrow \sigma'_2 \Rightarrow \sigma'_1 =_{\leq l} \sigma'_2$$



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Thus: every program  $c$  guarantees non-interference at level  $l_c = \bigsqcup \{sl(x) \mid x \in \mathit{Var}_c\}$

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### Example 19.5 (Interference (cf. Example 19.1))

1.  $c_1 = (\text{low} := \text{high})$  does not guarantee non-interference at level **low**:

- let  $\sigma_i = [\text{low} \mapsto 0, \text{high} \mapsto i]$  for  $i = 1, 2$  (and thus  $\sigma_1 =_{\leq \text{low}} \sigma_2$ )
- then  $\langle c_1, \sigma_1 \rangle \rightarrow \sigma'_1$  and  $\langle c_1, \sigma_2 \rangle \rightarrow \sigma'_2$  with  $\sigma'_i(\text{low}) = i$  ( $i = 1, 2$ )
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  - thus  $\sigma'_1 \neq_{\leq \text{low}} \sigma'_2$ .
2. Similarly:  $c_2 = (\text{if high} = 1 \text{ then low} := 1 \text{ else low} := 2 \text{ end})$  does not guarantee non-interference at level **low**

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  - thus  $\sigma'_1 \neq_{\leq \text{low}} \sigma'_2$ .
2. Similarly:  $c_2 = (\text{if high} = 1 \text{ then low} := 1 \text{ else low} := 2 \text{ end})$  does not guarantee non-interference at level **low**
3. Both programs guarantee non-interference at level **high**

# A Security Type System

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## Handling Explicit and Implicit Flows

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- Approach to deal with **implicit flows**: parametrise typing rules with security level of Boolean expressions (“`if high = 1`”) that guard the current command (“`then low := 1`”)



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- **Well-typedness predicate** for  $l \in SL$  and  $c \in Cmd$ :

$$l \vdash c$$

Meaning: “In the context of Boolean expressions of level (at most)  $l$ , command  $c$  is well-typed.”

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- Hence: assignments to variables of level  $< l$  are **forbidden** in  $c$

# A Security Type System

## The Security Type System

### Definition 19.6 (Well-typedness of commands)

For  $I \in SL$  and  $c \in Cmd$ ,  $I \vdash c$  is given by

$$\frac{}{(s\text{-skip}) I \vdash \text{skip}} \quad \frac{\text{sl}(x) \geq \text{sl}(a) \quad \text{sl}(x) \geq I}{(s\text{-asgn}) I \vdash x := a}$$

$$\frac{I \sqcup \text{sl}(b) \vdash c_1 \quad I \sqcup \text{sl}(b) \vdash c_2}{(s\text{-if}) I \vdash \text{if } b \text{ then } c_1 \text{ else } c_2 \text{ end}}$$

$$\frac{I \vdash c_1 \quad I \vdash c_2}{(s\text{-seq}) I \vdash c_1 ; c_2} \quad \frac{I \sqcup \text{sl}(b) \vdash c}{(s\text{-wh}) I \vdash \text{while } b \text{ do } c \text{ end}}$$

# A Security Type System

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$$\begin{array}{c} \text{(s-skip)} \frac{}{I \vdash \text{skip}} \quad \text{(s-asgn)} \frac{\text{sl}(x) \geq \text{sl}(a) \quad \text{sl}(x) \geq I}{I \vdash x := a} \quad \text{(s-seq)} \frac{I \vdash c_1 \quad I \vdash c_2}{I \vdash c_1 ; c_2} \\ \text{(s-if)} \frac{I \sqcup \text{sl}(b) \vdash c_1 \quad I \sqcup \text{sl}(b) \vdash c_2}{I \vdash \text{if } b \text{ then } c_1 \text{ else } c_2 \text{ end}} \quad \text{(s-wh)} \frac{I \sqcup \text{sl}(b) \vdash c}{I \vdash \text{while } b \text{ do } c \text{ end}} \end{array}$$

### Example 19.7

Let  $SL = \{\text{low}, \text{high}, \text{secret}\}$  (on the board) with  $\text{low} < \text{high} < \text{secret}$ .

1.  $\text{low} \vdash \text{if } \text{high} = \text{low} \text{ then } \text{high} := 1 \text{ else skip end}$
2.  $\text{low} \not\vdash \text{if } \text{high} = \text{low} \text{ then } \text{low} := 1 \text{ else skip end}$
3.  $\text{high} \vdash \text{if } \text{high} = \text{low} \text{ then } \text{high} := 1 \text{ else skip end}$
4.  $\text{secret} \not\vdash \text{if } \text{high} = \text{low} \text{ then } \text{high} := 1 \text{ else skip end}$

# A Security Type System

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## Confinement

The following lemma states that if  $l \vdash c$ , then  $c$  cannot modify variables of level  $< l$ , i.e., the effect of  $c$  is **confined** to variables of level  $\geq l$ :

### Lemma 19.8 (Confinement)

Let  $c \in \text{Cmd}$  and  $l \in \text{SL}$  such that  $l \vdash c$ . Then for all  $\sigma, \sigma' \in \Sigma$  with  $\langle c, \sigma \rangle \rightarrow \sigma'$ ,

$$\sigma =_{<l} \sigma'$$

Proof.

omitted □

# A Security Type System

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## Soundness

The following theorem states that the security type system is sound, i.e., that well-typedness guarantees non-interference at all levels:

### Theorem 19.9 (Non-interference)

*Let  $c \in \text{Cmd}$  such that  $\text{min } SL \vdash c$ , and let  $l \in SL$  and  $\sigma_1, \sigma_2, \sigma'_1, \sigma'_2 \in \Sigma$  such that  $\sigma_1 =_{\leq l} \sigma_2$ ,  $\langle c, \sigma_1 \rangle \rightarrow \sigma'_1$ , and  $\langle c, \sigma_2 \rangle \rightarrow \sigma'_2$ . Then  $\sigma'_1 =_{\leq l} \sigma'_2$ .*

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### Proof.

omitted □

The following example shows that the type system is incomplete, i.e., rejects some programs that guarantee non-interference:

### Example 19.10

```
low  $\not\vdash$  if high = 1 then low := 1 else low := 1 end
```



# A Security Type System

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## Extensions

- Does non-interference really guarantee absence of information flow?
  - problem: **covert channels**
  - example: `c = while high = 1 do skip end`
  - then  $\text{min } SL \vdash c$
  - but non-termination of `c` allows to conclude that `high = 1`
- Other kinds of covert channels: processing time, power consumption, ...

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- **Encryption** breaks traditional non-interference as (public) ciphertexts do depend on (confidential) contents
  - example:  $\text{low} := \text{encrypt}(\text{high})$
  - then  $\sigma_1(\text{high}) \neq \sigma_2(\text{high})$  (usually) implies  $\sigma'_1(\text{low}) \neq \sigma'_2(\text{low})$  after assignment
  - thus  $\sigma'_1 \not\leq_{\text{low}} \sigma'_2$  (interference)

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- Solution: relaxed notions of (non-)interference that distinguish between
  - breaking non-interference because of **legitimate use of (sufficiently strong) encryption** and
  - breaking non-interference due to an **(unintended) leak**(“possibilistic non-interference”)

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- Excellent survey paper:
  - A. Sabelfeld, A.C. Myers: Language-Based Information-Flow Security. IEEE Journal on Selected Areas in Communications, 21(1), 2003, 5–19*