



# Concurrency Theory WS 2015/2016

## — Series 2 —

Hand in until November 16 before the exercise class.

### Exercise 1 (CCS and LTS's)

(3+1 Points)

- (a) Decide whether the following CCS process definitions induce infinite LTS's and whether their trace languages are regular. Justify your answers.
- i)  $B = (B \parallel B) + a.nil$
  - ii)  $D = a.(D \parallel b.nil)$
  - iii)  $B = (B \parallel B) \setminus \{a\} + a.nil$
- (b) Prove or disprove: If a CCS process  $C$  is defined as  $C = P$  where  $C \parallel P'$  occurs as a subterm in  $P$ <sup>1</sup>, then  $LTS(C)$  is infinite.

### Exercise 2 (Complementation of HML Formulae)

(2+1+1 Points)

- (a) Suppose it holds for some arbitrary but fixed HML formula  $F$  that  $\llbracket F^c \rrbracket = S \setminus \llbracket F \rrbracket$  for every LTS  $(S, Act, \rightarrow)$ . Prove that  $\llbracket ([\alpha]F)^c \rrbracket = S \setminus \llbracket [\alpha]F \rrbracket$ .
- (b) Prove or disprove:  $(F^c)^c$  and  $F$  is semantically equivalent for every HMF formula  $F$ .
- (c) Prove or disprove:  $(F^c)^c$  and  $F$  is syntactically equivalent for every HMF formula  $F$ .

### Exercise 3 (Construction of HML Formulae)

(1+1+1 Points)

Let  $A = a.b.d.nil + a.c.d.nil$  and  $B = a.(b.d.nil + c.d.nil)$ .

- (a) Construct an HML formula which is satisfied by both  $A$  and  $B$ !
- (b) Construct an HML formula which is satisfied by  $B$  but not by  $A$ !
- (c) Construct an HML formula which is satisfied by  $A$  but not by  $B$ !

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<sup>1</sup> $P$  and  $P'$  are process expressions.