

# Theoretical Foundations of the UML - SS 2020

## — Exercise Sheet 10 —

Hand in until Monday July 6, 09:00 am via RWTHmoodle

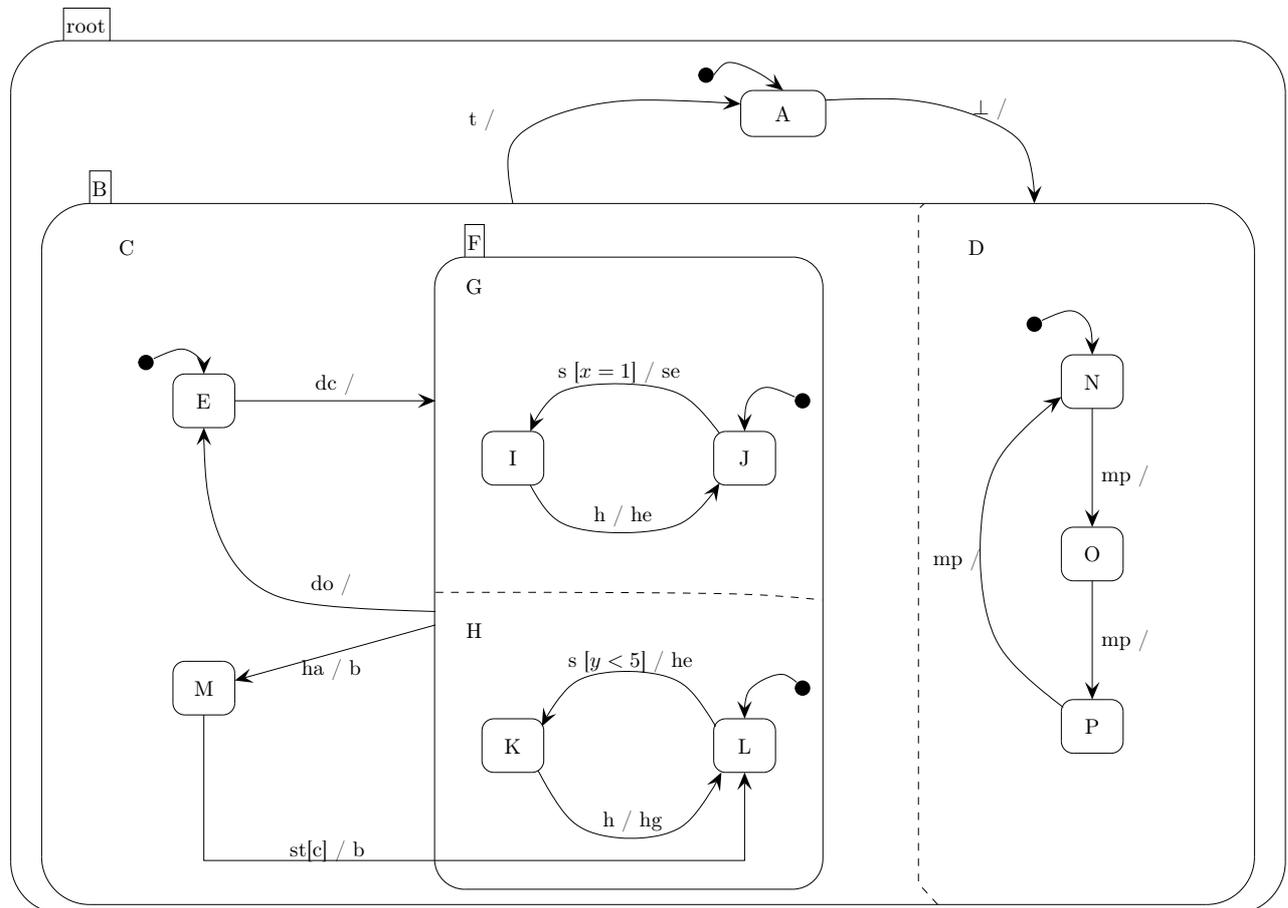
### General Remarks

- Questions regarding the lectures and exercises, if any, are expected in the Q&A session via Zoom, with the next on Thursday July 2, at 16:00. Zoom ID: 369 366 110, Password: FUML-QA.
- In this assignment an edge label of the form  $e/e'$  in a statechart  $SC$  indicates that  $SC$  is consuming the event  $e$  and executing an action that sends the event  $e'$  to  $SC$  (i.e., to itself).

### Exercise 1 (Ingredients of Statecharts)

(1+1+1 Points)

Consider the following statechart  $SC_1 := (N, E, Edges)$ .

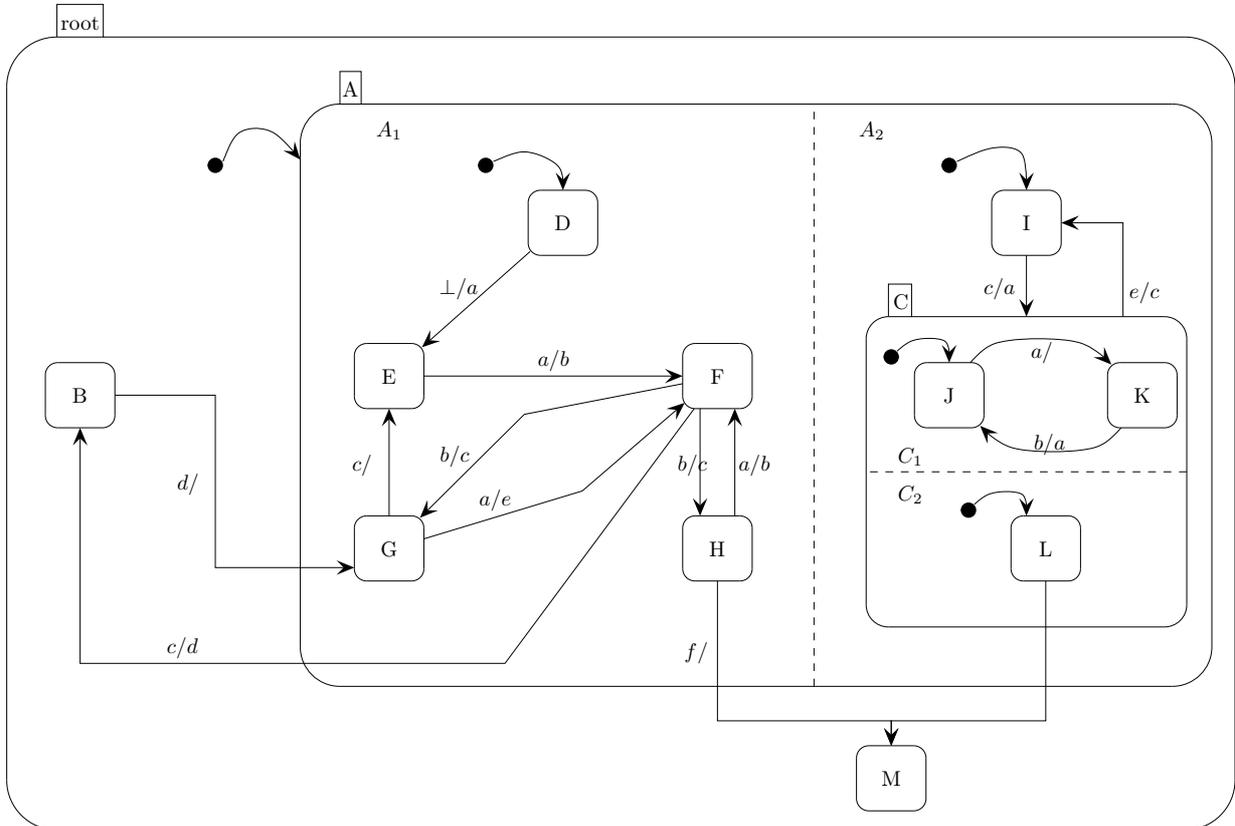


- 1) Give the formal description of  $SC_1$  by specifying its components  $(N, E, Edges)$ .
- 2) Construct the tree that represents the node hierarchy of  $SC_1$ .
- 3) Determine the types of the nodes in  $SC_1$ .

## Exercise 2 (Macro-Step Semantics)

(1+1+1+1 Points)

Consider the following stand-alone statechart  $SC$  (i.e., there are no statecharts running in parallel to  $SC$ ).

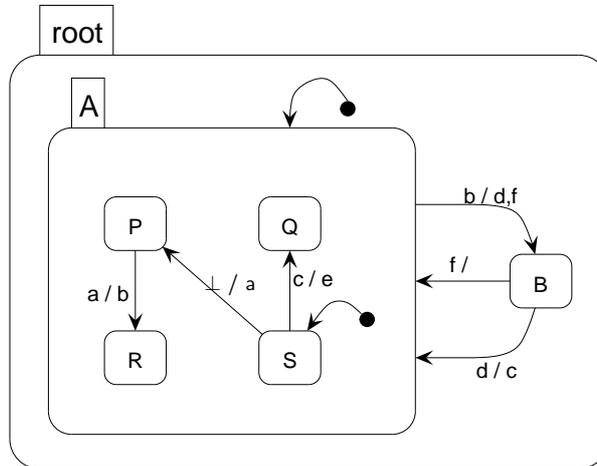


- Determine two example configurations  $c_1$  and  $c_2$  of  $SC$ . The configurations shall contain at least three nodes. Moreover, give two distinct example states  $s_i$  and  $s'_i$  for the configuration  $c_i, i \in \{1, 2\}$  (i.e., provide four example states in total). As there are no variables considered in  $SC$ , you may omit the variable valuation from each state.
- Calculate the sets of enabled edges  $En(s)$  of all states  $s$  determined in 1).
- Determine the scopes of the edges:
  - $\{H, L\} \rightarrow \{M\}$
  - $\{B\} \rightarrow \{G\}$
  - $\{C\} \rightarrow \{I\}$
- List at least two examples of pairs of inconsistent edges and two examples of pairs of consistent (and distinct) edges.

### Exercise 3 (Statecharts to a Mealy Machine)

(7 Points)

Consider the following statechart  $SC_1$ .



Determine the formal semantics of  $SC_1$  by constructing the underlying Mealy machine  $\mathcal{A} := (Q, q_0, \Sigma, \delta, \omega)$  through the following steps.

- 1) determine the initial state  $q_0$ .
- 2) determine the enabled edges  $En(q_0)$ .
- 3) determine every possible  $nextStep(q_0)$ .
- 4) determine the successor state  $\delta(q_0, E')$  for each set of event  $E' \subseteq E$  for which a corresponding macro step exists.
- 5) repeat these steps for each successor state.

When all states and their successors are determined, draw the resulting Mealy machine.

We assume that  $\delta(q, E')$  is defined only if there is a macro step  $T \subseteq En(q)$  for which  $E'$  is the set of trigger events of the edges in  $T$ . As there are no variables considered in  $SC_1$ , you may omit the variable valuation from each state.