

Exercise 1 (Regular Languages).

(13 points)

- (i) Give a regular expression that describes the language

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$$L := \{w \in \{0, 1\}^* \mid w = 0 \text{ or } w \text{ ends with } 00\}$$

- (ii) Give a nondeterministic finite automaton, possibly with
- ϵ
- transitions (
- ϵ
- NFA), that recognises the language which is given by the regular expression

3

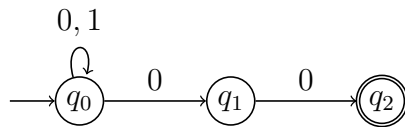
$$\alpha := (11 + 0)^*(00 + 1)^*$$

- (iii) Show that the automaton constructed in (ii) accepts the word
- $w := 1101$
- .

1

- (iv) Apply the powerset construction to turn the following nondeterministic finite automaton (NFA)
- \mathfrak{A}
- into a deterministic finite automaton (DFA)
- \mathfrak{A}'
- .

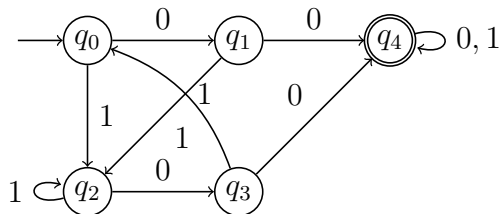
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- (v) Minimise the following deterministic finite automaton (DFA)
- \mathfrak{A}
- .

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(Reminder: the minimal DFA is obtained by merging equivalent states. Here, two states are considered equivalent if they accept the same outgoing words.)



Exercise 2 (Context-Free Languages).

(12 points)

- (i) Give a context-free grammar
- G
- which generates the language

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$$L := \{a^i b^j c^k \mid i, j, k \geq 1 \text{ and } (i \neq j \text{ or } j \neq k)\}.$$

- (ii) Give a derivation of the word
- $aabcc \in L$
- from the start symbol of
- G
- .

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- (iii) Let
- G'
- be the following context-free grammar:

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$$S \rightarrow SA \mid a$$

$$A \rightarrow BS$$

$$B \rightarrow BB \mid BS \mid b \mid c$$

and let $w := acbaa$. Employ the CYK-Algorithm to show that $w \in L(G')$. Use the following table to compute the sets

$$N_{i,j} := \{A \in N \mid A \Rightarrow^* w[i,j]\} \quad (1 \leq i \leq j \leq 5)$$

where $w[i,j] := a_i \dots a_j$ for $w = a_1 a_2 a_3 a_4 a_5$.

$i \backslash j$	1	2	3	4	5
1					
2	X				
3	X	X			
4	X	X	X		
5	X	X	X	X	